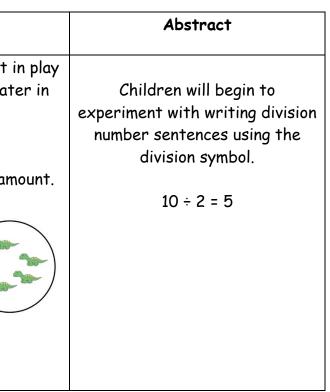


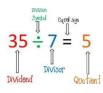
Foundation Stage

Key Vocabulary: sharing, halving, number patterns

Objective & Strategy	Concrete	Pictorial
To begin to divide by sharing.	Children will use a range of resources to share concrete resources to begin to demonstrate understanding.	Children will understand equal groups and share items out in and problem solving. They will count in 2s and 10s and late 5s.
	Children will start with an even number and will need to share this out equally in a given group. e.g. 10 ÷ 2 = 5	Step 1: Count how many you have. Step 2: Share them equally so each group has the same am Step 3: Count how many are in each group. Image: Count how many are in each group. Image: Count how many are in each group.







<u>Year 1</u>

Key Vocabulary: division, dividing, grouping, sharing, doubling, halving, array, number pattern, equal grouping, equal sharing

Objective & Strategy	Concrete	Pictorial
To divide by	Children will use concrete resources, including uni-fix cubes	Children will draw jottings and have pictorial representations to
sharing	to share into equal groups. Children will also be able to half	demonstrate knowledge of sharing into equal groups.
5	a number up to 20 by sharing into equal groups.	
To half a		12 ÷ 2 = 6
number up to		
20.		I know there are 2 groups and in each group there are 6 flowers.
	<u>Stem Sentence:</u> I know there are <u>2</u> groups so I can share <u>12</u> counters which will equal <u>6</u> in each group.	12 ÷ 2 = 6
		10
		12



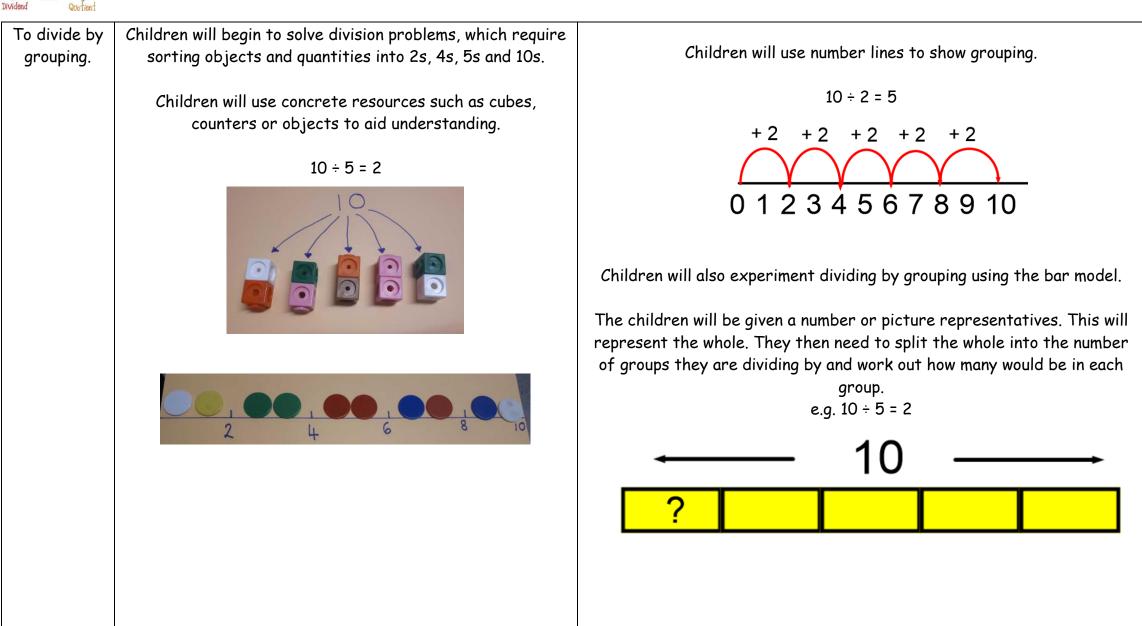
Abstract

Children will be introduced to word problems to solve division problems.

6 sweets are shared between 2 people. How many do they have each?

Stem Sentence: I know <u>12</u> divided equally between <u>2</u> groups' equals <u>6</u>.

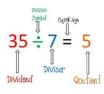






There are 10 flower bulbs. Plant 2 in each pot. How many pots are there?

There are 10 flower bulbs. Plant 5 in each pot. How many pots are there?



<u>Year 2</u>

Key Vocabulary: multiplication, multiply, multiplied by, multiple, grouping, doubling, array, row, column, groups of, times once, twice, three times ... ten times, repeated addition, one each, two each, three each ... ten each, equal groups of, multiplication table, multiplication fact.

Objective & Strategy	Concrete	Pictorial	
To divide by sharing.	Children will use a range of concrete resources, including cubes to share objects and quantities into equal groups. I have 12 cubes, can you share them equally into 3 groups?	<image/> <text><text><text><text></text></text></text></text>	



Abstract

Children will be writing division number sentence using the divide symbol.

12 ÷ 3 = 4

12 ÷ 4 = 3



To divide by grouping	Children will begin to solve division problems, which	Children will use number lines to show grouping	The
(repeated addition)	require sorting objects and quantities into 2s, 4s, 5s and 10s. Children will use concrete resources such as cubes, counters or objects to aid understanding.	A set of the s	The
To use related multiplication and division facts using the inverse for the 2, 3, 5 and 10 times table.	Children will use concrete resources, including cubes to represent arrays. These will then form part of the learning process to explain number related facts and begin to write these in number form. $2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 2 = 4$ $8 \div 4 = 2$	Children will use pictorial representations to solve missing number facts that demonstrate related facts. $ \begin{array}{c} $	S



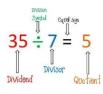
nere are 12 flower bulbs. Plant 3 in each pot. How many pots are there?

nere are 12 flower bulbs. Plant 4 in each pot. How many pots are there?

Children will show all 8 related number sentences to demonstrate related facts.

$$2 \times 4 = 8$$

 $4 \times 2 = 8$
 $8 \div 2 = 4$
 $8 \div 4 = 2$
 $8 = 2 \times 4$
 $8 = 4 \times 2$
 $2 = 8 \div 4$
 $4 = 8 \div 2$



<u>Year 3</u>

Key Vocabulary: groups of times, repeated addition, division, dividen, divided by, divided into left, left over, remainder grouping sharing, share, share equally one each, two each, three each ... ten each group in pairs, threes ... tens equal groups of, halving, array row, column, number patterns, division fact

Children continue to deepen their understanding of the link between multiplication and division and use physical objects to find related facts. $3 \times 6 = 18$ $18 \div 3 = 6$ $6 \times 3 = 18$ $18 \div 6 = 3$ $6 \times 3 = 18$ $18 \div 6 = 3$	Children represent an array pictorially then find the associated multiplication and division facts by sorting into equal groups. $18 \div 3 = 6$ 3x6 = 18 $18 \div 6 = 3$ 6x3 = 18	Children apply th relationships to statements. 3 × 6 = 6 × 3 = 18 ÷ 3 18 ÷ 6 They use associo each number rep multiplier multiplicand p
		3 × 6 = 18
Children will use concrete resources, including place value counters to divide by grouping. 96÷8=12	Children will continue to use repeated addition on the number line but will work with increasingly large numbers.	ofgroups eachgroup There are 96 f Ho
 Step 1: Use place value counters to create the dividend. The step 2: Look at the divisor, this explains the number of groups you will need. E.g. 8. The children will need to exchange 1 ten for 10 ones. The step 3: Children will need to share out the remaining 	96 ÷ 8 = 12 Children will count on from in 8s from 0 until they reach 96. +8 +8 +8 +8 +8 +8 +8 +8 +8 +8 +8 +8 0 8 16 24 32 40 48 56 64 72 80 88 96 Children will also continue to use the bar model to support their understanding.	There are 96 f Ha Hov How r
	counters to divide by grouping. 96÷8=12 Step 1: Use place value counters to create the dividend. 10 10 10 10 10 10 10 10 FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF	counters to divide by grouping. 96+8=12 Step 1: Use place value counters to create the dividend. 10 10 10 10 10 10 10 10 groups you will need. E.g. 8. The children will need to exchange 1 ten for 10 ones. 5tep 3: Children will need to share out the remaining step 3: Children will need to share out the remaining



their understanding of inverse o write related multiplication and division = 18 18 = 3 x 6 = 18 18 = 6 × 3 3 = 6 6= 18 ÷ 3 3= 18 ÷ 6 6 = 3 ciated vocabulary correctly and know what epresents in the calculation. dividend divisor quotient product 18 $18 \div 3 = 6$ 1 Ť 1 number number number in number in all of groups each group in all footballs. Each player needs 8 footballs. How many players are there? 96 ÷ 8 = 12 footballs. Each player needs 12 footballs. How many players are there? 96 ÷ 12 = 8 ow many groups 8 are in 96? many groups of 12 are in 96?



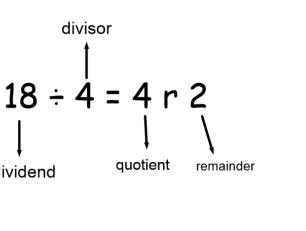
	10 10 10 10 10 10 10 10 1		
To use arrays to divide.	Children will link division to multiplication by using arrays. They will begin writing numbers sentences to show what they can create.	- .	
To divide with whole numbers and represent remainders.	Children will use a range of concrete resources to divide between groups and see what is left over.	Children will use a number line to jump forward in equal jumps. They will then see how many more they need to jump to find the remainder.	Children will con using the d
	18 ÷ 4 = 4 r 2	$18 \div 4 = 4 r 2$	1 div

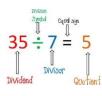


ill find the inverse of multiplication and nces by creating linking number sentences.

6 x 4 = 24 4 x 6 = 24 24 ÷ 6 = 4 24 ÷ 4 = 6

omplete written division number sentences division symbol and r to represent the remainder.





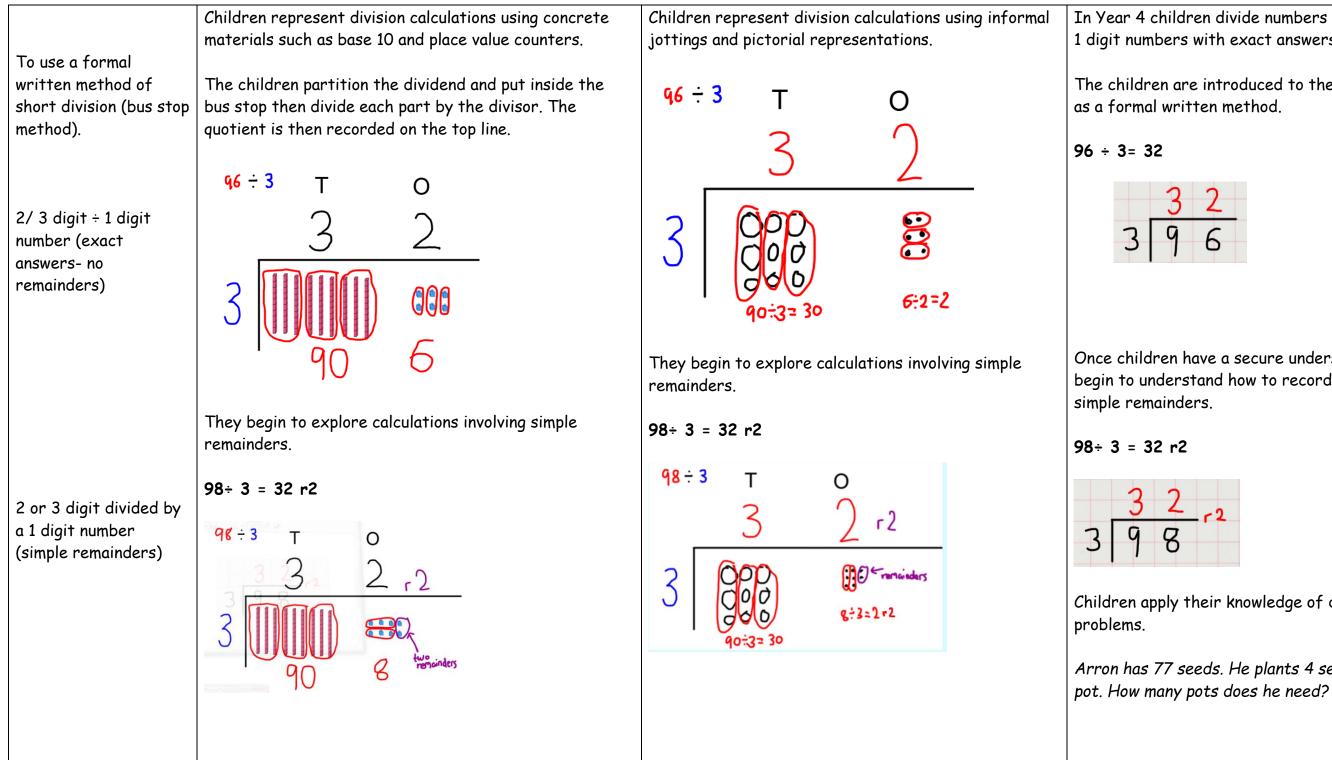
<u>Year 4</u>

Key Vocabulary: factors, multiples, groups of, share, share equally, equal groups, division, divide, divided by, divided into, left, left over, remainder, array.

Objective & Strategy	Concrete	Pictorial	Abstract
To recall multiplication and division facts for multiplication tables up to 12x 12.	Children continue to deepen their understanding of the link between multiplication and division and use physical objects to find related facts. $3 \times 6 = 18$ $18 \div 3 = 6$ $6 \times 3 = 18$ $18 \div 6 = 3$	Children represent an array pictorially then find the associated multiplication and division facts by sorting into equal groups. $18 \div 3 = 6$ 3x6 = 18 3x6 = 18 $18 \div 6 = 3$ 6x3 = 18	Children apply their understanding of inverse relationships to write related multiplication and division statements. $3 \times 6 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 3 = 6$ $6 = 18 \div 3$ $18 \div 6 = 3$ $3 = 18 \div 6$ They use associated vocabulary correctly and know what each number represents in the calculation. multiplier multiplicand product divisor quotient $3 \times 6 = 18$ $18 \div 3 = 6$ $7 \uparrow 1$ $18 \div 3 = 6$ $7 \uparrow 1$ $18 \div 3 = 6$ $7 \uparrow 1$ $18 \div 3 = 6$
To recognise and use factor pairs and commutativity in mental calculations.	Children use physical objects to create arrays to support their understanding of factors. Factors of 24	Children investigate finding all factors of a number by drawing arrays. Factors of 24 2X12 3X8 4X6 1,2,3,4,6,8,12 and 24.	Children use their knowledge of multiplication and division facts to find factors of numbers. Factors of 24 1 × 24 = 24 2 × 12= 24 3 × 8 = 24 4 × 6 = 24









In Year 4 children divide numbers up to 3 digits by a 1 digit numbers with exact answers.

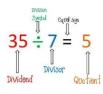
The children are introduced to the bus stop method

2	2
3	4
G	6
	0

Once children have a secure understanding, they begin to understand how to record calculations with

Children apply their knowledge of division to word

Arron has 77 seeds. He plants 4 seeds in each plant



<u>Year 5</u>

Key Vocabulary: factors, multiples, groups of, share, share equally, equal groups, division, divide, divided by, divided into, left, left over, remainder, array, prime numbers, composite numbers.

Objective & Strategy	Concrete	Pictorial	Abstract
To recall multiplication and	Children continue to deepen their understanding of the link between multiplication and division and use physical objects to find related facts.	Children represent an array pictorially then find the associated multiplication and division facts by sorting into equal groups.	Children apply their understanding of inverse relationships to write related multiplication and di statements. $3 \times 6 = 18$ $18 = 3 \times 6$
division facts for multiplication tables up to 12x 12.	3 x 6= 18 18 ÷ 3 = 6 6 x 3 = 18 18 ÷ 6 = 3		$6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 3 = 6$ $6 = 18 \div 3$ $18 \div 6 = 3$ $3 = 18 \div 6$
		18÷3=6 18÷6=3 3×6=18 6×3=18	They use associated vocabulary correctly and know each number represents in the calculation. $\begin{array}{c} \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $
To recognise and use factor pairs of a number and find common factors of two numbers.	Children use physical objects to create arrays to support their understanding of factors. Find the common factors of 18 and 24 Factors of 24 Factors of 18 Factors of 18 F	Children investigate finding factors by drawing arrays to find all solutions. They then find factors which belong to both numbers. Find the common factors of 18 and 24 Factors of 24 2X12 2X12 3X8 4X6 1,2,3,4,6,8,12 and 24. Factors of 18 7x0 7xe factors ore 1,2,3,6,9,18 The common factors are 1, 2, 3 and 6.	Children use multiplication and division facts to fir factors of numbers. Find the common factors of 18 and 24 Factors of 18 Factors of 24 (1) \times 18 (1) \times 24 (2) \times 9 (2) \times 12 (3) \times 6 (3) \times 8 (4) \times 6 G.C.F. The common factors are 1, 2, 3 and 6.



division

- now what
- find



			This three-digit n
			Write another thr
To establish	Children find prime numbers and composite (non-prime numbers) by using arrays. They understand that composite numbers form arrays and prime numbers cannot be arranged into arrays.	Children use jottings and pictorial representations to investigate composite and prime numbers. Prime Numbers 7	Children use t find the prime numbers that all prime numb
whether a number up to 100 is prime and recall prime numbers up to 19.			(1) 12 (1) 14 15 24 22 (2) 24 28 (3) 32 33 34 35 (4) 42 (4) 44 45 51 52 53 54 55
	9 7 composite prime number number	0000 0000 000 Hmm hon-arrayable.	60 52 53 54 54 70 72 73 74 75 84 82 83 84 85 94 92 93 94 95



umber has 2 and 7 as factors.

294

ree-digit number which has 2 and 7 as factors.

their knowledge of multiples and factors to e numbers up to 100. They eliminate have factors other than 1.They can recall bers up to 19

)(ers	up	то	19	•
)	×	0	×	X	X
C	¥¢	0	78	19	20
ζ	26	27	28	2	30
ζ	36	37	38	3 9	340
í,	46	@	48	ৠ	<u>,50</u>
Ļ	56	2	58	9	60
ζ	66	ଡ	68	<u>)</u> 69	X
ζ	76	X	78	0	30
	86	3 87		89	90
ζ	96	୭	<u>98</u>)	<u>)</u> 00(

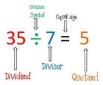


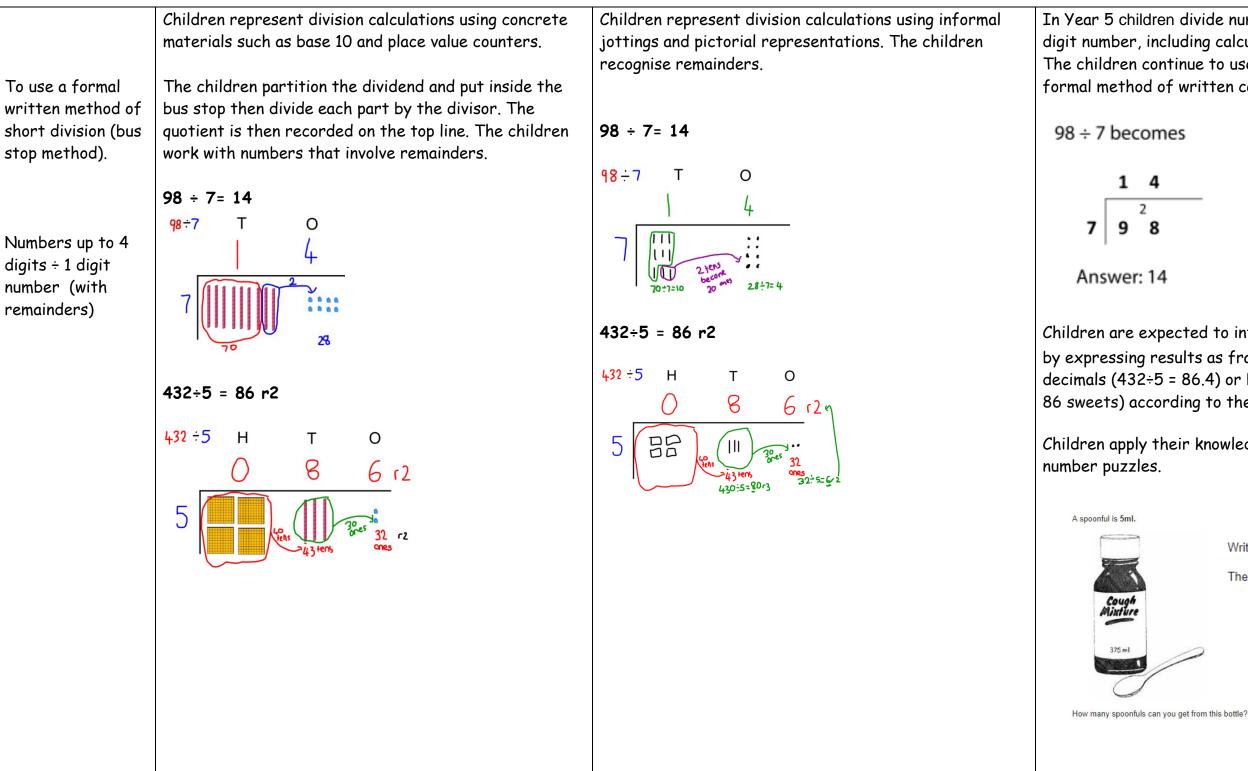
Ta divida uda da	Children use resources to understand what 10, 100 and 1000 times bigger looks like.	Children use place value grids to divide numbers by 10, 100 and 1000s. They understand the movement of the digits on the place value grid.	Children apply t numbers by 10, 1
To divide whole numbers and those involving decimals by 10, 100 and 1,000	3 is ten times smaller than 30. 30 is ten times smaller than 300. 3 is one hundred times smaller than 3. 300	$\frac{\text{Dividing}}{\text{igits move RIGHT 1 space}}$ $\div 10 \qquad \text{digits move RIGHT 2 spaces}$ $\div 1000 \qquad \text{digits move RIGHT 3 spaces}$ $345 - 100 = 3.45$ $1000 \qquad 100 \qquad 10$	3450÷ 10 = 345 345÷100= 3.45 2.67 ÷10= 0.267 12.7÷1000= 0.01 They apply their puzzles and wor Circle the number that
		They apply this knowledge to decimal numbers. $4.12 \div 10 \simeq 0.412$ 10 000 100 10 10 1 1 10 1000 $0.412 \checkmark$	9,700 Write the missing 75 ÷ A PS4 is on for usually costs£4



their knowledge of place value to divide), 100 and 1000, including decimal numbers. 15 5 57 .0127 eir understanding to more complex number ord problems. at is 10 times greater than nine hundred and seven. 9,070 907 9,007 970 ing number to make this division correct. = 7.5 or sale at a tenth of its original price. It

450.90. How much is it at the sales?







In Year 5 children divide numbers up to 4 digits by a 1 digit number, including calculations involving remainders. The children continue to use the bus stop method as a formal method of written calculation.

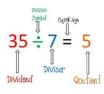
omes	432 ÷	5	beco	me	s	
4			8	6	r 2	
8	5	4	3	2		

Answer: 86 remainder 2

Children are expected to interpret non-integar answers by expressing results as fractions $(432 \div 5 = 86 \frac{2}{5})$, decimals $(432 \div 5 = 86.4)$ or by rounding $(432 \div 5 = 86.4 \approx 86 \text{ sweets})$ according to the context.

Children apply their knowledge using word problems and number puzzles.

Write in the missing digit. The answer does not have a remainder. $3 \int \frac{2}{8} \frac{6}{8}$



<u>Year 6</u>

Key Vocabulary: factors, multiples, groups of, share, share equally, equal groups, division, divide, divided by, divided into, left, left over, remainder, array

Objective & Strategy	Concrete	Pictorial	Abstract
To recall multiplication and division facts for multiplication tables up to 12x 12.	Children continue to deepen their understanding of the link between multiplication and division and use physical objects to find related facts. $3 \times 6 = 18 18 \div 3 = 6 \qquad 6 \times 3 = 18 18 \div 6 = 3$	Children represent an array pictorially then find the associated multiplication and division facts by sorting into equal groups. $18 \div 3 = 6$ 3x6 = 18 3x6 = 18 $18 \div 3 = 18$	Children apply their understanding of inverse relatives write related multiplication and division statement $3 \times 6 = 18$ $6 \times 3 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 6 = 3$ $18 \div 6 = 3$ $18 \div 6 = 3$ They use associated vocabulary correctly and known number represents in the calculation.
To identify common factors.	Children use physical objects to create arrays to support their understanding of factors. Find the common factors of 18 and 24 Factors of 24 Factors of 18 Factors of 18 F	Children investigate finding all factors of a number by drawing arrays. They then find factors which are the same in both numbers. Find the common factors of 18 and 24 Factors of 24 $2^{\chi_{12}}$ $3^{\chi_{8}}$ $4^{\chi_{6}}$ $1^{\chi_{2}}$ $3^{\chi_{8}}$ $4^{\chi_{6}}$ $1^{\chi_{2}}$ $3^{\chi_{8}}$ Factors of 18 $3^{\chi_{8}}$ $1^{\chi_{18}}$ $5^{\chi_{9}}$ $1^{\chi_{18}}$ $1^{\chi_{18}}$ $3^{\chi_{9}}$ $1^{\chi_{18}}$ $1^{\chi_{18}}$	Children use their knowledge of multiplication and facts to find factors of numbers. Find the common factors of 18 and 24 Factors of 18 Factors of 24 (1) \times 18 (1) \times 24 (2) \times 9 (2) \times 12 (3) \times 6 (3) \times 8 (4) \times 6 (6.C.F. The common factors are 1, 2, 3 and 6.

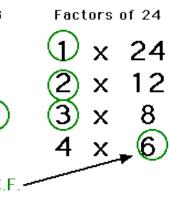


1.			
1.			
	,		
	7	•	

elationships to ents. 6 3 3 6

now what each

and division





		The common factors are 1, 2, 3 and 6.	
To establish whether a number up to 100 is prime and recall prime numbers up to 19.	Children find prime numbers and composite (non-prime numbers) by using arrays. They understand that composite numbers form arrays and prime numbers cannot be arranged into arrays.	Children use jottings and pictorial representations to investigate composite and prime numbers. Prime Numbers	Children use thei knowledge of mul and factors to fi prime numbers u They eliminate no that have factors than 1. They can r prime numbers u
To use a formal written method of short division (bus stop method). Larger numbers ÷ 1 digit number (involving remainders)	Children represent division calculations using concrete materials such as base 10 and place value counters. The children partition the dividend and put inside the bus stop then divide each part by the divisor. The quotient is then recorded on the top line. The children work with numbers that involve remainders. $98 \div 7= 14$ $98 \div 7= 14$ $98 \div 7= 14$	Children represent division calculations using informal jottings and pictorial representations. The children will recognise remainders. $98 \div 7 = 14$ $98 \div 7 = 14$ $98 \div 7 = 14$ $7 \qquad \qquad$	with calculations to use the bus st calculation. $98 \div 7$ becomes 1 4 7 9 8 Answer: 14 Children are expension expressing result (432 \div 5 = 86 4) or
	432÷5 = 86 r2	432÷5 = 86 r2	Children apply th number puzzles.



eir nultiples find the up to 100. numbers ors other n recall all up to 19.

1	2	3	X	3	×	0	X	X	ÞC
1	X	13	14	3 5	¥¢	ⓓ	38	19	20
24	72	23	24 K	25	26	27	28	29	30
31	3 2	3 3	34	35	36	37	38	≫ ર્	34 0(
(41)	42	4 3	'44 '	45	46	(1)	48	ৠৠ	<u>`</u> 50
3 1	5Z	63	34	35	,56	57	58	ම)60
61	76Z	<u>63</u>	64	65	<u>766</u>	ଡ	68	<u>)69</u>	X
7	X	03	74	75	76	X	78	0	>80
<u>81</u>	8 2	83	84	85	86	3 87	38	89	9 0
>শ	92	ঙ্গ	94	<u>95</u>	96	୭	98	<u>99</u>	100

ren divide larger numbers by a 1 digit number ns involving remainders. The children continue stop method as a formal method of written

Answer: 86 remainder 2

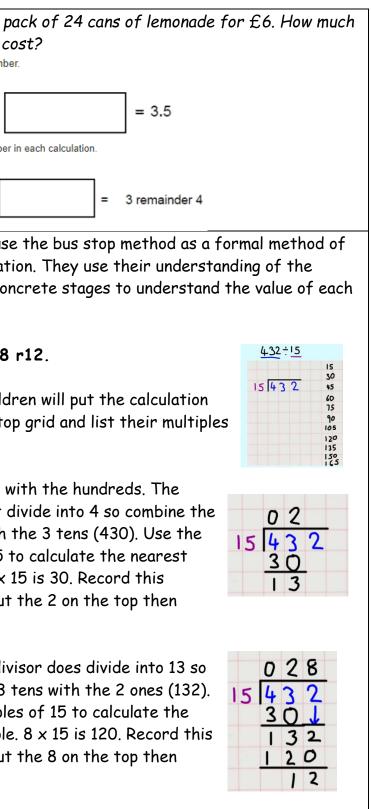
spected to interpret non-integar answers by ults as fractions (432÷5 = 86 $\frac{2}{5}$), decimals or by rounding (432÷5 = 86.4 ≈ 86 sweets) we context.

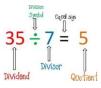
their knowledge using word problems and 3.



	432÷5 н 5	-43 tens	0 6 r 2 32 r 2 cnes r 2	5	÷5 H	1291 430-2	5=80r3	[2] - 32: 5= €r2		Sharon buys a pa does each can co. Write the missing number. 70 ÷
To use a formal written method of long division (bus stop method). Divide larger numbers ÷ 2 digit numbers (involving remainders)	materials such as bo The children partiti	ase 10 and p on the divid :h part by th	ulations using concrete lace value counters. end and put inside the b ne divisor. The quotient 0 8 rl2 130 132 rl2	jot s 43	•	H	T 2	ions. 0 8 130 130 132 ones	r12 r12	The children use written calculation pictorial and construmber. 432 ÷ 15 = 28 m Step one: Children into the bus stop of the divisor. Step 2: Start windivisor doesn't di 4 hundred with t multiples of 15 to multiple. Two x 12 underneath, put to subtract. Step 3: The division combine the 13 to Use the multiples nearest multiple. underneath, put to subtract.







	Step 4: The num remainder, recor answer 432 ÷ 15
	Children are exp expressing resul decimals (432÷15 cars) according f



umber left is your cord this with your 15 = 28 r12.

		0	0		15
	0	2	8	r 2	30
15	4	3	2		45
	3	0	1		60
	1	3	2		75
	1	2	0		90 105
		1	2		105
					120
					135
					150

xpected to interpret non-integar answers by sults as fractions (432÷15 = $28\frac{12}{15}$ = $28\frac{4}{5}$), ÷15 = 28.8) or by rounding (432÷15 = 28.8 ≈ 29 g to the context.